FUZZY TOPOLOGICAL DIGITAL SPACE OF FLAT ELECTROENCEPHALOGRAPHY DURING EPILEPTIC SEIZURES

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FUZZY TOPOLOGICAL DIGITAL SPACE OF FLAT ELECTROENCEPHALOGRAPHY DURING EPILEPTIC SEIZURES

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ABSTRACT

Epileptic seizures are manifestations of epilepsy caused a temporary electrical disturbance in a group of brain cells. Electroencephalography (EEG) is a recording of electrical activity of the brain and it contains valuable information related to the different physiological states of the brain. Flat EEG (fEEG) was developed to compress and analyze information in the brain during epileptic seizures obtained from EEG signal. In this study, the fEEG is made in digital form by using Voronoi digitization. Khalimsky fuzzy topology and fuzzy topological digital space is constructed to be used in studying properties fuzzy topology of fEEG. It is obtained that fEEG is a fuzzy topological digital space and τ-connected.

Keywords: Flat EEG, Fuzzy Topological Digital Space, Khalimsky Fuzzy Topology

1. INTRODUCTION

Epilaptic seizures are manifestations of epilepsy caused a temporary electrical disturbance in a group of brain cells (neurons). The recording of electrical signals emanated from the human brain, which can be collected from the scalp of the head is called Electroencephalography (EEG). Careful analysis of the EEG records can provide new insights into the epileptogenic process and may have considerable utilization in the diagnosis and treatment of epilepsy (Tahir, 2010).

The methods in information apmetry were developed by Amari and Nagaoka (2000) as early since 1993. It has gain a big momentum when dealing with statistical data. On the other hand, (Zakaria, 2008) has developed a novel method to map high dimensional signal, namely EEG signal into low dimensional space (MC). The process is a transformation of EEG signals originating from the patient's head into two dimensional planes. The result of the transformation

of the EEG signals into low-dimensional space is called as flat EEG (fEEG). fEEG has been used purely for visualization, but the main scientific value will lie in the ability of flattening method to preserve information. The 'jewel' of the fEEG method is EEG signals can be compressed and analyzed.

Nazihah et al. (2009) have constructed fEEG as a digital space. They proved that the digital space of the fEEG is an Alexsandroff space and have applied relational topology in order to incorporate topological space of real time recorded EEG signal with digital fEEG. This construction is a key foundation of fEEG which has linked with the idea of fuzzy information granulation. All points in digital fEEG which give the coordinate of the location of the current source are supposed to be in the structure of discrete objects. It means that each of the points possesses smallest neighborhood in analogy of digital topology. It can be a point or a small portion of region which contains several points that caused the dysfunction of brain. Thus, every

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pint is said to be integer grid on the plane. These points can also carry information such as magnetic field and images (Nazihah, 2009)

2. MATERIALS AND METHODS

2.1. Flat EEG Digital

fEEG is digitized into grid by using Voronoi digitization (Kiselman, 2004), as follows:

Let $x \in \mathbb{R}$, $p \in \mathbb{Z}$ then the Voronoi cell with nucleus p is Equation (1):

$$V_0(p) = \{ x \in \mathbb{R} \mid \forall q \in \mathbb{Z}, d(x,p) \le d(x,q) \}$$
 (1)

On the x-axis of the fEEG, the Voronoi cell is Equation (2):

$$3$$

$$Vo(p) = \left\{ x \in \mathbb{R} \mid p - \frac{1}{2} < x \le p + \frac{1}{2}, p \in \mathbb{Z} \right\}$$

$$(2)$$

Each $x \in \mathbb{R}$ is a member in only one Voronoi cell Vo(p) for every $p \in \mathbb{Z}$, so that the *x*-axis Voronoi digitization of the fEEG has the following form Equation (3):

$$\frac{5}{\text{dig}[\{x\}]} = \left\{ p \in \mathbb{Z} | x \in \text{Vo}(p) \right\} \tag{3}$$

JEEG is the Tartesian product of the x-axis and y-axis, so that the digitization of the fEEG is the Cartesian product of the digitization of the x-axis and y-axis, namely Equation (4):

$$\operatorname{dig}\left[\left\{\left(x,y\right)\right\}\right] = \left\{\left(p_{x},p_{y}\right) \in \mathbb{Z}^{2} | x \in \operatorname{Vo}(p_{x}), y \in \operatorname{Vo}(p_{y})\right\}$$
(4)

Where:

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$$Vo(p_x) = \left\{ x \in \mathbb{R} \mid p_x - \frac{1}{2} < x \le p_x + \frac{1}{2}, p_x \in \mathbb{Z} \right\}$$

And:

$$\operatorname{Vo}(p_y) = \left\{ y \in \mathbb{R} | p_y - \frac{1}{2} < y \le p_y + \frac{1}{2}, p_y \in \mathbb{Z} \right\}$$

Hence, the fEEG in digital form Equation (5):

$$fEEG = \left\{ (p, Volt) \mid p = (p_x, p_y) \in \mathbb{Z}^2; Volt \in \mathbb{R}^+ \right\}$$
$$= \left\{ (x, y)_{volt} \mid x, y \in \mathbb{Z}; Volt \in \mathbb{R}^+ \right\}$$
 (5)



With volt is electric potential.

2.2. Alexandroff Fuzzy Topological Space

Alexandroff topological space (Kopperman, 2003) is extended to fuzzy topological space and presented formally as follows.

Definition 1

Let $(X, \tilde{\tau})$ be a fuzzy topological space, then $(X, \tilde{\tau})$ is called Alexandroff fuzzy topological space if the intersection of any open fuzzy set in X is open, i.e.:

If
$$\tilde{A}_i \in \tilde{\tau}$$
 then $\left(\bigcap_i \tilde{A}_i\right) \in \tilde{\tau}$, for $\left\{\tilde{A}_i \mid i \in I\right\}$

The smallest neighborhood (Kiselman, 2004) is extended to fuzzy topology on X.

Definition 2

Let $(X,\tilde{\tau})$ be a fuzzy topological space. The smallest neighborhood of $c{\in}X$ (with respect to $\tilde{\tau}$) is defined by:

$$S_{\tilde{\tau}}(c) = \bigcap_{\tilde{U} \in \tilde{\tau}} \tilde{U} = \min_{\tilde{U} \in \tilde{\tau}} \left(\mu_{\tilde{U}}(c) \right)$$

Theorem 1

Let $(X, \tilde{\tau})$ be a fuzzy topological space, then $(X, \tilde{\tau})$ is an Alexandroff fuzzy topological space if and only if $\forall x \in X$, x possesses the smallest open neighborhood, i.e., $\forall x \in X$, $\tilde{S}_{\tilde{\tau}}(x) = \bigcap_{x \in X} \tilde{U}$ is an open fuzzy set in X.

Proof

Suppose $(X, \tilde{\tau})$ is an Alexandroff fuzzy topological space with $x{\in}X$. Consider $N(x)=\left\{\tilde{N}\subset X\,|\,\tilde{N}\text{ is an open neighborhood of }x\right\}$. Pick $\tilde{S}(x)=\cap\tilde{N}$ for $\tilde{N}\in N(x)$, then $\tilde{S}(x)$ is an open fuzzy set because X is an Alexandroff fuzzy topological space. Hence, $\tilde{S}(x)$ is an open neighborhood of x. Based on the intersection definition, it is clear that $\tilde{S}(x)$ is a smallest open neighborhood of x.

Suppose $\forall x \in X$, x has the smallest open neighborhood $\tilde{S}(x)$. Let $\tilde{V} = \bigcap_i \tilde{U}_i$ be an arbitrary intersection of open set, where, \tilde{U}_i is open in X. If $\tilde{V} = \emptyset$ then V is open and we are done. If $\tilde{V} \neq \emptyset$ and pick $x \in \tilde{V}$, then $x \in \tilde{U}_i, \forall i \in I$ so that $\tilde{S}(x) \subseteq \tilde{U}_i, \forall i \in I$ because $\tilde{S}(x)$ is the smallest open fuzzy set containing x. Therefore, $\tilde{S}(x) \subseteq \tilde{V}$. Hence, \tilde{V} is open because it contains an open set around each of its points.

2.3. Khalimsky Fuzzy Topological on Z and Z²

Khalimsky topology τ_z (Melin, 2008) is extended to fuzzy topology on Z. The construction of the fuzzy topological is done by a collection of fuzzy sets that is a base that will generate a fuzzy topology.

Let $\tilde{B}(n)$ be a fuzzy set on Z as follows Equation (6):

$$\begin{split} \tilde{B}(n) &= \\ &\left\{ \left(n, \mu_{\tilde{B}(n)}(n) \right\} \text{ iif n is odd} \\ &\left\{ \left(n - 1, \mu_{\tilde{B}(n)}(n-1) \right), \left(n, \mu_{\tilde{B}(n)}(n) \right), \\ &\left(n + 1, \mu_{\tilde{B}(n)}(n+1) \right) \\ \end{matrix} \right\} \text{iif n is even} \end{split}$$

Collection of the fuzzy sets $\tilde{B}(n)$, $n \in \mathbb{Z}$ is denoted by $\tilde{\beta} = \left\{ \tilde{B}(n) \mid n \in \mathbb{Z} \right\}$ and collection of all possible union of elements of $\tilde{\beta}$ is denoted by $\tilde{\tau} = \left\{ \bigcup \boldsymbol{\varepsilon} \mid \boldsymbol{\varepsilon} \subset \tilde{\beta} \right\}$

Theorem 2

 $(\mathbb{Z}, \tilde{\tau})$ is a fuzzy topological space

Proof

We use definition of fuzzy topological space in (Srivastava et al., 1981):

- Pick 𝔭 = Ø , then 𝔭 = Ø ⊂ β̃ , so that ∪Ø = Ø.
 Hence, Ø ∈ τ̃ . Therefore, τ̃ contain constant fuzzy set
- Let $\tilde{A}_1, \tilde{A}_2 \in \tilde{\tau}$ with $\tilde{A}_1 = \bigcup_i \tilde{B}(n_{1i})$, $\tilde{A}_2 = \bigcup_j \tilde{B}(n_{2j})$ and $\tilde{B}(n_{1i})$, $\tilde{B}(n_{2i}) \in \tilde{\beta}$

$$\begin{split} &\left(\tilde{\mathbf{A}}_{1} \cap \tilde{\mathbf{A}}_{2}\right) \\ &= \left(\bigcup_{i} \tilde{\mathbf{B}}(\mathbf{n}_{1i})\right) \cap \left(\bigcup_{i} \tilde{\mathbf{B}}(\mathbf{n}_{2j})\right) = \bigcup_{i,j} \left(\left(\tilde{\mathbf{B}}(\mathbf{n}_{1i})\right) \cap \left(\tilde{\mathbf{B}}(\mathbf{n}_{2j})\right)\right) \end{split}$$

There are two possible results of finite intersection of element $\tilde{\beta}$, i.e.,

$$\begin{split} \left(\tilde{\mathbf{B}}(\mathbf{n}_{i_1}) \cap \tilde{\mathbf{B}}(\mathbf{n}_{2j})\right) &= \varnothing \quad \text{or} \quad \left(\tilde{\mathbf{B}}(\mathbf{n}_{i_1}) \cap \tilde{\mathbf{B}}(\mathbf{n}_{2j})\right) \in \tilde{\boldsymbol{\beta}} \text{, so that} \\ (\tilde{\mathbf{A}}_1 \cap \tilde{\mathbf{A}}_2) &= \bigcup \varnothing = \varnothing \in \tilde{\boldsymbol{\tau}} \quad \text{or} \quad (\tilde{\mathbf{A}}_1 \cap \tilde{\mathbf{A}}_2) = \bigcup_k \tilde{\mathbf{B}}(\mathbf{n}_k) \quad \text{where} \\ \tilde{\mathbf{B}}(\mathbf{n}_k) \in \tilde{\boldsymbol{\beta}} \text{. Hence, } (\tilde{\mathbf{A}}_1 \cap \tilde{\mathbf{A}}_2) \in \tilde{\boldsymbol{\tau}} \end{split}$$

$$\begin{split} \bullet & \quad \text{Let} \quad \{\tilde{A}_i\}, \forall i \!\in\! I \quad \text{where} \quad \tilde{A}_i \!\in\! \tilde{\tau} \;, \quad \text{with} \\ \tilde{A}_i = \!\bigcup_j \tilde{B}(n_{1j}), \tilde{A}_2 = \!\bigcup_j \tilde{B}(n_{2j}), ...; \qquad \tilde{B}(n_{ij}) \!\in\! \tilde{\beta} \;, \bigcup_i \tilde{A}_i = \\ \tilde{A}_i \cup \tilde{A}_2 \cup ... = \!\! \left(\bigcup_j \tilde{B}(n_{ij}) \right) \!\! \left| \bigcup \! \left(\bigcup_j \tilde{B}(n_{2j}) \right) \!\! \right| \! \cup ... = \\ \bigcup_i \! \left(\bigcup_j \tilde{B}(n_{ij}) \right) \! = \! \bigcup_{i,j} \tilde{B}(n_{ij}) \end{aligned}$$

Therefore, $\bigcup_i \tilde{A}_i$ can be expressed as union of element $\tilde{\beta}$. Hence, $\bigcup_i \tilde{A}_i \in \tilde{\tau}$.

Fuzzy topology $\tilde{\tau}$ in Theorem 2 is called as Khalimsky fuzzy topology, denoted by $\tilde{\tau}_{\mathbb{Z}}$ and $(\mathbb{Z}, \tilde{\tau}_{\mathbb{Z}})$ is called Khalimsky fuzzy topological space. Z together with $\tilde{\tau}_{\mathbb{Z}}$ is called as Khalimsky fuzzy line.

Theorem 3

 $(\mathbb{Z}^{22}, \tilde{\tau}_{\mathbb{Z}^2})$ is a fuzzy topological space

Proof

Since $(\mathbb{Z}, \tilde{\tau}_{\mathbb{Z}})$ is a fuzzy topological space then $\tilde{\tau}_{\mathbb{Z}^{22}}$ is a fuzzy topology generated by family $\left\{A_j \times B_k \mid A_j, B_k \in \tilde{\tau}_{\mathbb{Z}}\right\}$ (Palaniappan, 2005), so that $(\mathbb{Z}^{22}, \tilde{\tau}_{\mathbb{Z}^2})$ is a fuzzy topological space.

The topology $\tilde{\tau}_{\mathbb{Z}^2}$ on Z^2 is called as Khalimsky fuzzy topology on Z^2 and Z^2 together with $\tilde{\tau}_{\mathbb{Z}^2}$ is called Khalimsky fuzzy plane.

The elements of the family $\left\{A_{j} \times B_{k} \mid A_{j}, B_{k} \in \tilde{\tau}_{\mathbb{Z}}\right\}$ as follows Equation (7):

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 $\tilde{B}(p) =$

$$\begin{cases} \left\{ (p,\mu_{\tilde{B}(p)}(p)) \right\} & \text{if p is pure open} \quad e \quad n \\ \left\{ (p^{-*},\mu_{\tilde{B}(p)}(p^{-*})),(p,\mu_{\tilde{B}(p)}(p)),(p^{**},\mu_{\tilde{B}(p)}(p^{**})) \right\} \\ \text{or} & \text{if p is mixed} \\ \left\{ (p^{-*},\mu_{\tilde{B}(p)}(p^{-*})),(p,\mu_{\tilde{B}(p)}(p)),(p^{**},\mu_{\tilde{B}(p)}(p^{**})) \right\} \\ \\ \left\{ (p,\mu_{\tilde{B}(p)}(p)),(p^{**},\mu_{\tilde{B}(p)}(p^{**})),(p^{-*},\mu_{\tilde{B}(p)}(p^{**})), \\ (p^{**},\mu_{\tilde{B}(p)}(p^{**})),(p^{**},\mu_{\tilde{B}(p)}(p^{**})),(p^{-*},\mu_{\tilde{B}(p)}(p^{-*})), \\ (p^{-*},\mu_{\tilde{B}(p)}(p^{**})),(p^{**},\mu_{\tilde{B}(p)}(p^{**})),(p^{-*},\mu_{\tilde{B}(p)}(p^{-*})) \\ \end{cases} \\ \text{if p is pure closed} \end{cases}$$

with
$$p = (x,y) \in \mathbb{Z}^2$$
; $p^{++} = (x+1, y+1)$; $p^+ = (x-1, y+1)$; $p^+ = (x,y+1)$; $p^+ = (x+1,y-1)$; $p^- = (x-1, y-1)$; $p^+ = (x+1,y)$; $p^- = (x-1,y)$.

Based on the definition 2, Theorem 1 and properties of $\tilde{B}(p)$, we have the following corollaries:

Corollary 1

 $\tilde{B}(p)$ is the smallest open neighborhood of p.

Corollary 2

A Khalimsky fuzzy topological space $(\mathbb{Z}, \tilde{\tau}_{\mathbb{Z}})$ is an Alexandroff fuzzy topological space.

On the Khalimsky fuzzy plane, $\tilde{B}(p)$ is the smallest open neighborhood of p on the plane (Corollary 1), so that $\tilde{B}(p)$ define adjacency $\rho_{\tilde{\tau}_{2^2}}$ on Z^2 (Herman, 1998), i.e., $\forall p, q \in Z^2$ then $(p,q) \in \rho_{\tilde{\tau}_{2^2}}$ if and only if $p \neq q$ and $p \in \tilde{B}(q)$ or $q \in \tilde{B}(p)$. The adjacency induced by Khalimsky fuzzy topology $\tilde{\tau}_{g^2}$ is called Khalimsky adjacency.

2.4. Fuzzy Topological Digital Space

Topological digital space (Herman, 1998) is extended to fuzzy topology and it is called fuzzy topological digital space

Definition 3

Let V be any set and π is an adjacency on V. A digital space (V,π) is called fuzzy topological digital

space if there exist a fuzzy topology $\tilde{\tau}$ on V, such that for any fuzzy set \tilde{A} in V, if \tilde{A} is π -connected then \tilde{A} is $\tilde{\tau}$ -connected (topologically connected)

Definition 4

Let $(X, \tilde{\tau})$ be a fuzzy topological space. The adjacency induced by fuzzy topology $\tilde{\tau}$, denoted $\rho_{\tilde{\tau}}$, is defined as: $(c,d) \in \rho_{\tilde{\tau}}$ if and only if $c \neq d$ and $c \in S_{\tau}(d)$ or $d \in S_{\tau}(c)$, $\forall c$, $d \in X$.

Theorem 4

Let $(X, \tilde{\tau})$ be an Alexandroff fuzzy topological space and \tilde{A} is any fuzzy set on X, then \tilde{A} is $\rho_{\tilde{\tau}}$ – connected if and only if \tilde{A} is $\tilde{\tau}$ – connected.

Proof

We prove it from the left, the rest is left.

Now we show that if there exist $\tilde{U}, \tilde{V} \in \tilde{\tau}$ such that $\tilde{U} \cap \tilde{A} \neq \emptyset$, $\tilde{V} \cap \tilde{A} \neq \emptyset$ and $\tilde{A} \subset (\tilde{U} \cup \tilde{V})$ then $\min \left(\mu_{\Omega}(c_k), \mu_{\tilde{V}}(c_k), \mu_{\tilde{A}}(c_k) \right) \neq 0$ or $(\tilde{U} \cap \tilde{V} \cap \tilde{A}) \neq \emptyset$. Pick $c \in (\tilde{U} \cap \tilde{A})$ and $d \in (\tilde{V} \cap \tilde{A})$ then $c \in \tilde{A}$ and $d \in \tilde{A}$. Since \tilde{A} is $\rho_{\tilde{\tau}}$ - connected, there is a $\rho_{\tilde{\tau}}$ - path $\langle c = p_0, p_1, ..., p_n = d \rangle$ in \tilde{A} from c to d. Due to $\tilde{A} \subset (\tilde{U} \cap \tilde{V})$ (assumption), then there must be a k, $1 \le k \le n$ such that $p_{k-1} \in \tilde{U}$ or $\mu_{\tilde{l}}(p_{k-1}) \neq 0$ and $p_k \in p_k \in \tilde{V}$ or $\mu_{\tilde{V}}(p_k) \neq 0$. Since $(p_{k-1}, p_k) \in \rho_{\tilde{\tau}}$, either $p_{k-1} \in S_{\tilde{\tau}}(p_k)$ or $p_k\!\in\!S_{\bar{\tau}}(p_{k-1})$. We complete this first part of the proof assuming that the latter is the case; the proof of the alternative is strictly analogous. Since U is an open fuzzy set which contain pk-1, it follows from the definition of the smallest neighborhood that $S_{z}(p_{k-1}) \subset \tilde{U}$ and so $p_k \in \tilde{U}$ or $\mu_{\tilde{U}}(p_k) \neq 0$. Likewise, since $c, d \in \tilde{A}$ and $< c = p_0, p_1, ..., p_n = d > is a \rho_{\bar{\tau}}$ - path connected c and d in \tilde{A} then $p_k \in \tilde{A}$ or $\mu_{\tilde{A}}(p_k)\neq 0$. Hence, $\min \left(\mu_{\tilde{\mathbf{I}}}(\mathbf{c}_{k}), \mu_{\tilde{\mathbf{V}}}(\mathbf{c}_{k}), \mu_{\tilde{\mathbf{A}}}(\mathbf{c}_{k}) \right) \neq 0 \text{ or } (\tilde{\mathbf{U}} \cap \tilde{\mathbf{V}} \cap \tilde{\mathbf{A}}) \neq \emptyset.$

Theorem 5

Let $(V_{\mathfrak{F}})$ be an Alexandroff fuzzy topological space then $V, \rho_{\mathfrak{t}}$ is a fuzzy topological digital space if and only if V is $\tilde{\tau}$ -connected



Proof

Since $V, \rho_{\bar{\tau}}$ is a fuzzy topological digital space then $V, \rho_{\bar{\tau}}$ is a digital space. Therefore, V is $\rho_{\bar{\tau}}$ -connected (definition of digital space). By Theorem 4, V is $\bar{\tau}$ -connected. The same theorem implies that if this condition is satisfied, then $V, \rho_{\bar{\tau}}$ is necessarily a fuzzy topological digital space.

Corollary 3

If $(\mathbb{Z}^2, \tilde{\tau})$ is a Khalimsky fuzzy topological space then $(\mathbb{Z}^2, \rho_{\tilde{\tau}})$ is a digital space with $\rho_{\tilde{\tau}}$ as Khalimsky adjacency.

Corollary 4

If $(\mathbb{Z}^2, \tilde{\tau})$ is a Khalimsky fuzzy topological space and $\rho_{\tilde{\tau}}$ is an adjacency induced by $\tilde{\tau}$ then $(\mathbb{Z}^2, \rho_{\tilde{\tau}})$ is a fuzzy topological digital space.

3. RESULTS AND DISCUSSION

In this study, fEEG digitized as in (5) will be showed as a fuzzy topological digital space.

Theorem 6

fEEG is a Khalimsky fuzzy topological space.

Proof

Suppose $fEEG = \{(x,y)_{Vol} | x,y \in \mathbb{Z}; Volt \in \mathbb{Z}^*\}$ as mentioned in (5). However fEEG can be redefined as follows:

$$\begin{split} & \text{fEEG } = \left\{ \left(x, y \right)_{\text{Volt}} \mid x, y \in \mathbb{Z}; \text{ Volt} \in \mathbb{Z}^* \right\} \\ & = \left(\mathbb{Z}, \tilde{\tau}_{\mathbb{Z}} \right) \times \left(\mathbb{Z}, \tilde{\tau}_{\mathbb{Z}} \right) = \left(\mathbb{Z}^2, \tilde{\tau}_{\pi^2} \right) \end{split}$$

By the Theorem 3, $(\mathbb{Z}^2, \tilde{\tau}_{\mathbb{Z}^2})$ is a Khalimsky fuzzy topological space. Therefore, fEEG is a Khalimsky fuzzy topological space.

Corollary 5

fEEG is an Alexandroff fuzzy topological space.

Proof

By using Corollary 2 and Theorem 6.



Theorem 7

(fEEG, $\rho_{\tilde{\tau}_{a}}$) is a digital space

Proof

By using Corollary 3 and Theorem 6.

Theorem 8

(fEEG, $\rho_{\tilde{\tau}_{m2}})$ is a fuzzy topological digital space.

Proof

By using Corollary 4 and Theorem 6.

Theorem 9

fEEG is $\tilde{\tau}_{7^2}$ - connected

Proof

By using Theorem 8 and Theorem 5.

4. CONCLUSION

In this study, it is shown that fEEG during epileptic seizure is a Khalimsky fuzzy topological space, a fuzzy topological digital space and $\tilde{\tau}_{z2}$ – connected.

5. ACKNOWLEDGMENT

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